

## Outline

- **Introduction**
- **Classes of Location Problem**
- **Taxonomy of Location Problems**
- **Problem Description/ Formulation**
- **Solution Methods: Heuristics**
- **Future Investigations**

## Introduction

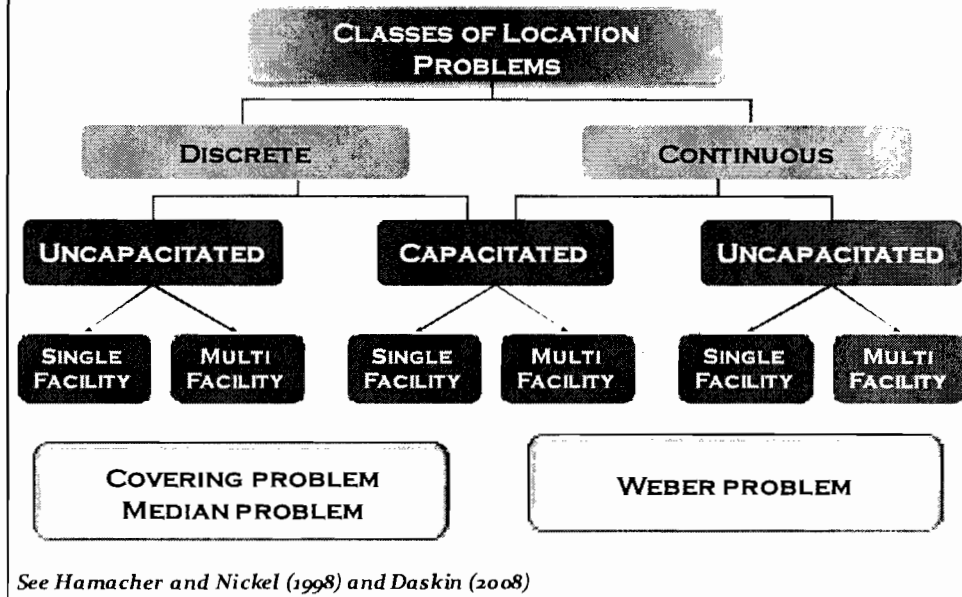
*Location analysis is concerned with determining the location of one/more facilities either on a plane or a network with respect to a set of existing facilities so as to perform one or more criteria as an objective function*

## Introduction

*The typical criteria may include:*

- minimizing average travel time or distance between origins and destinations,*
- minimizing average response time,*
- minimizing a cost function of travel or response time,*
- minimizing maximum travel time, or*
- maximizing minimum travel time*

## Classes of Location Problems: Basic



## General Questions

- *How many facilities should be built?*
- *Where should these facilities be?*
- *What should the size of the facility be?*
- *How should demand be allocated?*

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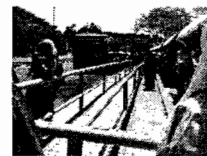
*The answers depend intensively on the perspective of what is the purposes and what are the aims embedded on the goal.*

## Taxonomy of Location Problems (I)

### DISCRETE LOCATION PROBLEMS

#### PUBLIC SECTORS

- police stations
- fire stations
- Ambulances, etc.
- In a small scale example is bus stops in UUM



*The facilities are sited as near as possible to the demand points*

## Taxonomy of Location Problems (2)

### DISCRETE LOCATION PROBLEMS

#### LOCATING OBNOXIOUS (UNDESIRABLE) FACILITIES

- Nuclear power plants
- Toxic dumps, solid waste repositories
- pollution producing industrial plants, etc.

↳ *the locations would tend to be as far as possible from resident dwelling centres.*

↳ *A possibility of damage property and/or loss of life*

## Taxonomy of Location Problems (3)

### DISCRETE LOCATION PROBLEMS

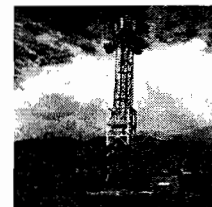
#### PRIVATE SECTORS

manufacturing / service companies:

- production and/ or assembly plants,
- distribution centres
- retail outlets.
- Base transceiver station
- Banks
- Courier agencies

**TESCO**  
Every little helps

**Giant**  
Every little helps

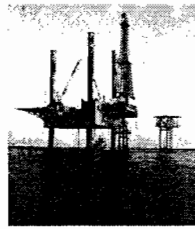


*Erroneous location decisions in this circumstance will increase costs and decrease competitive advantages of the company*

## Taxonomy of Location Problems (4)

### CONTINUOUS LOCATION PROBLEMS

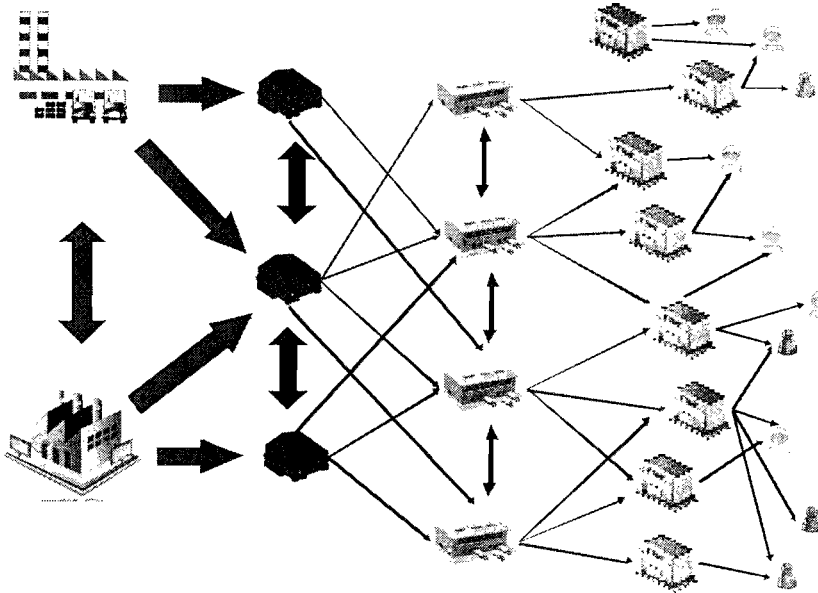
- Location of oil drills in the sea or the desert
- Space Satellites



## Importance of Location Analysis (1)

- The viewpoint of
  - Producers*
    - Reduce the operating cost and give more benefits
  - Customers*
    - obtain advantages, such as lower prices, better quality products and services
- The number of facilities to be located and the size of the individual facilities
  - *the trade off between the service and the cost*
- Facility location decisions also consider how to accommodate *various demand allocation policies*

## Importance of Location Analysis (2)



## Importance of Location Analysis (3)

- However, location analysis is not always concerned with large scale enterprises such as factories or warehouse locations
- *In the small scale units such as*
  - the location of machines within a production centre
  - the location of a router in a computer network
  - the location of components on a printed circuit board
  - the location of electrical safety devices on electrical network
  - the location of lecture classes within the university

## Problem Description

### To determine

- the number of facilities to open (public/private sectors),
- the locations (continuous/ discrete), the sizes, and
- the allocation of the customers to each of these open facilities.
  - so that total transportation costs are minimised
  
- **Given:**
  - The location of each customer point/ coordinate
  - The demand of every customer point
  - The transportation cost for the area of interest
  - The number of facilities to be opened

## Problem Description: Formulation

$$\text{Minimise } \sum_{i=1}^M \sum_{j=1}^n x_{ij} d(X_i, a_j) \quad (1)$$

Subject to

$$\sum_{i=1}^M x_{ij} = w_j, \quad j = 1, \dots, n \quad (2)$$

$$\sum_{j=1}^n x_{ij} \leq b, \quad i = 1, \dots, M \quad (3)$$

$$x_{ij} \geq 0, \quad i = 1, \dots, M; j = 1, \dots, n \quad (4)$$



## Solution Techniques

### ***Exact methods***

- It is advantageous when a problem is relatively small
- When the size of the problem increases, the computational time will grow exponentially

### ***Heuristic Approaches***

- **Do not guarantee optimality** but have the ability to produce **near optimal solutions** to difficult optimization problems in a reasonable amount of time

## Heuristic Techniques: Definition

- Reeves and Beasley (1993, p. 6) define heuristic as:

*"A heuristic is a technique which seeks good (i.e. near optimal) solutions at a reasonable computational cost without being able to guarantee either feasibility or optimality, or even in many cases to state how close to optimality a particular feasible solution is"*

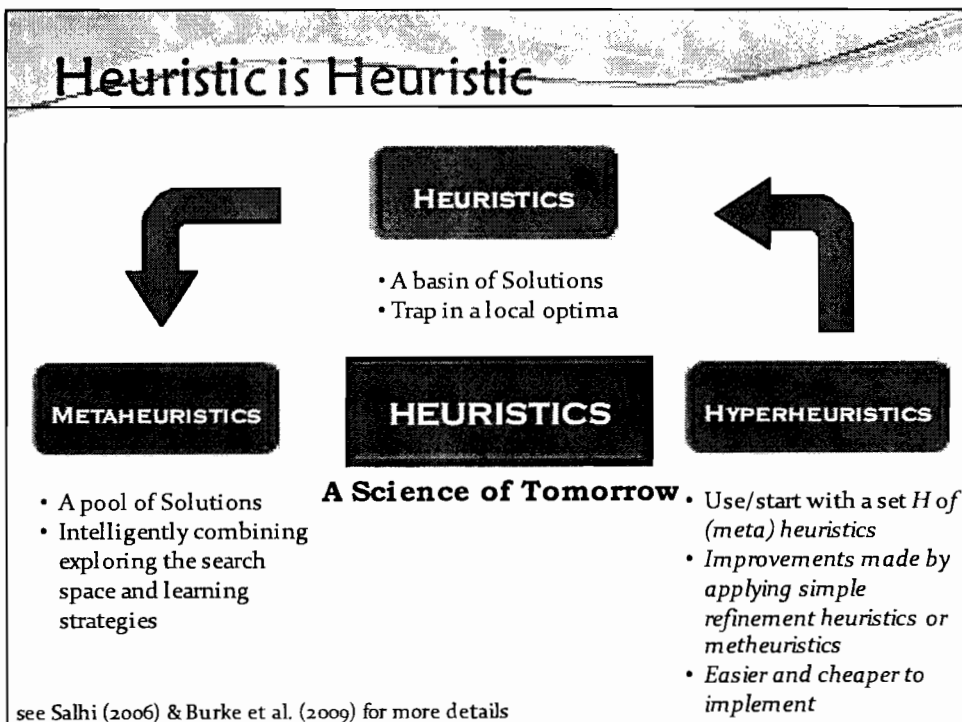
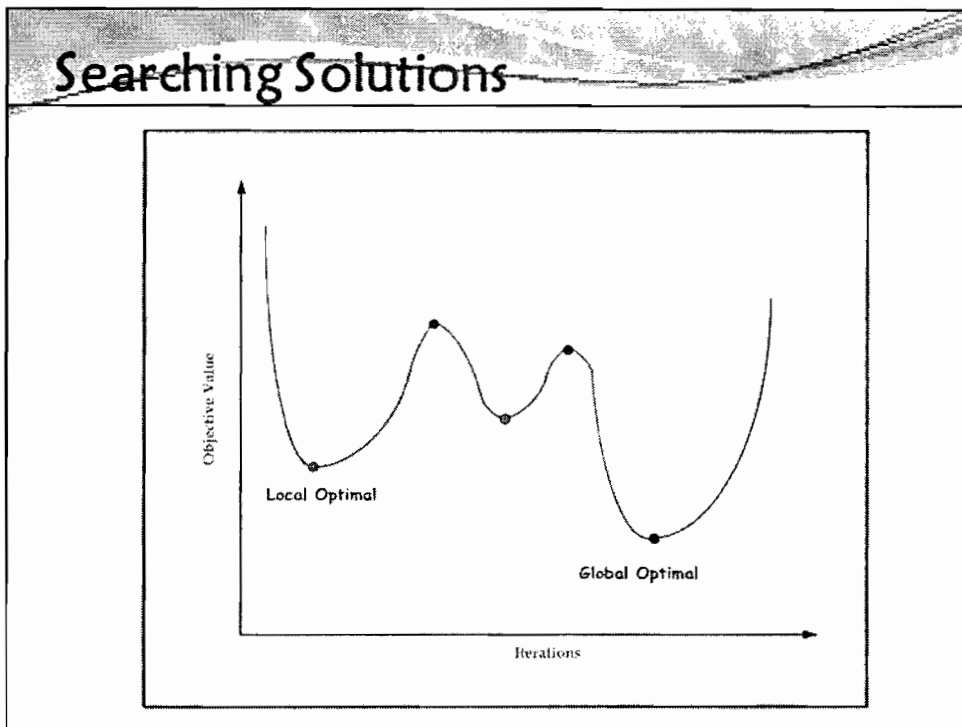
- Heuristic procedures are based on common sense, logic and experience
- They are capable of producing more than **one single solution** to the problem since they are easy to understand and to modify
- Interface in Artificial Intelligence and Operational Research

## Heuristic Techniques: Not limited to

- **Heuristics** (Osman & Laporte, 1996, Salhi, 2006)  
Constructive (descent/ perturbation/ multiphase approaches)
- **Metaheuristics** (Glover & Kochenberger, 2003)
  - Local search (tabu search, simulated annealing)
  - Population/ evolutionary based (*genetic algorithms, ant colony system, bee colony, particle swarm optimisation*)
  - Multistart Search (*greedy randomized adaptive search procedure*)
  - Neighbourhood Search (*Variable Neighbourhood Search*)
  - Mathematical based (*lagrangian heuristic*)
  - Human/ graphical interaction (*neural networks*)
- **Hyperheuristics** (Burke et al. 2009, Ozcan et al. 2008)  
*Use (meta) heuristics to choose (meta) heuristics*

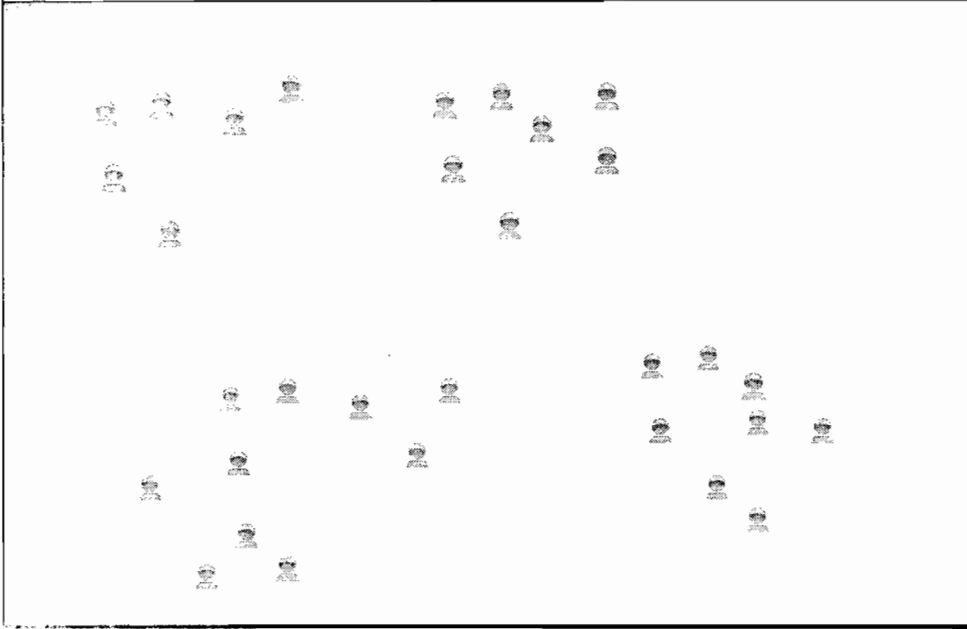
## A Basic Framework of Heuristics

- Step 1: Find an *initial solution*  $S$  and compute its objective value  $C(S)$
- Step 2: While there is an untested neighbour  $S' \in \epsilon$ , do the following (*improvement phase*):
  - Generate sequentially a trial  $S' \in \epsilon$  and compute  $C(S')$
  - If  $C(S') < C(S)$  then replace  $S$  as a current solution. Otherwise, retain  $S$  and repeat Step 2
- Step 3: *Terminate the search* and return  $S$  as the final solution

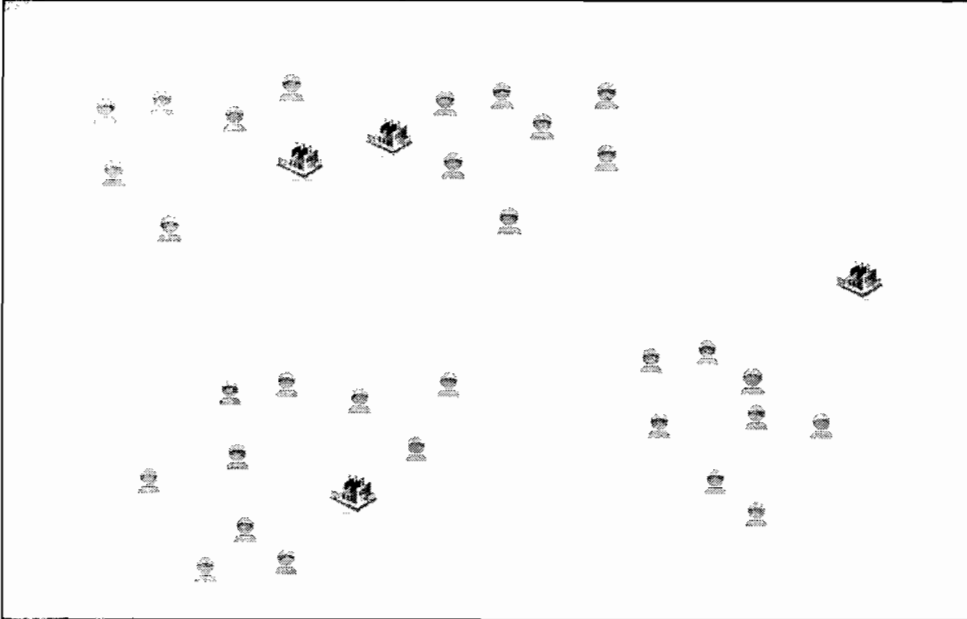


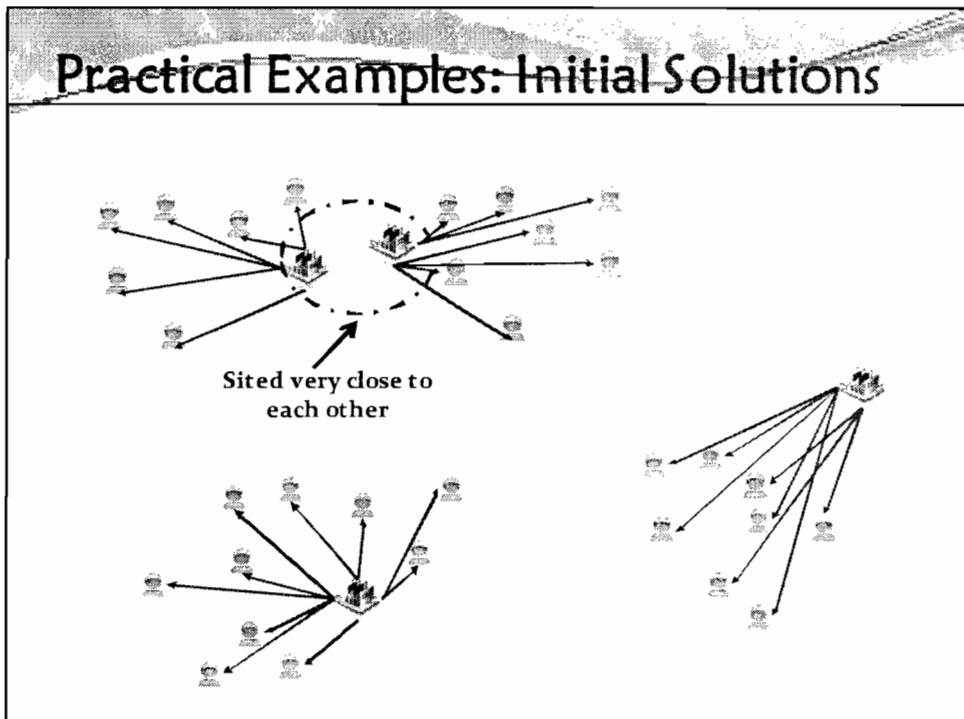
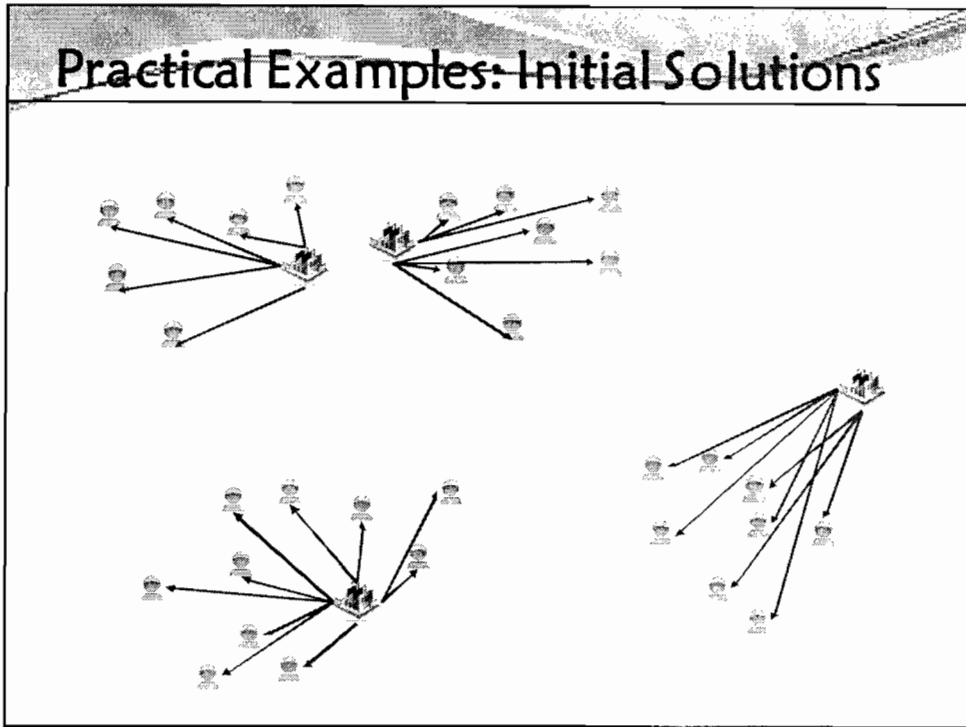
# Practical Examples

- Construct 4 facilities
- The objective is to minimise total transportation costs

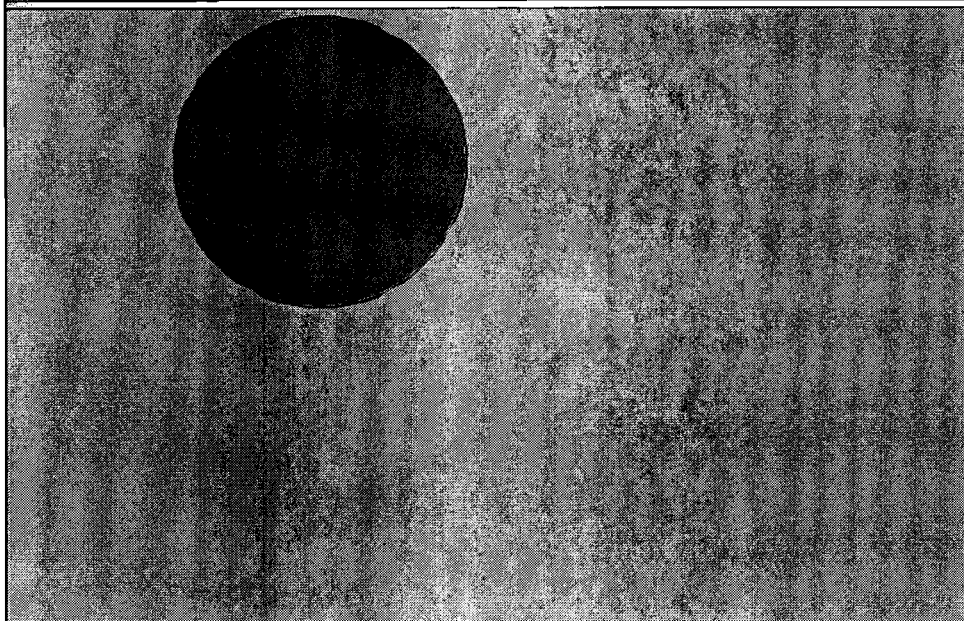


# Practical Examples: Initial Solutions



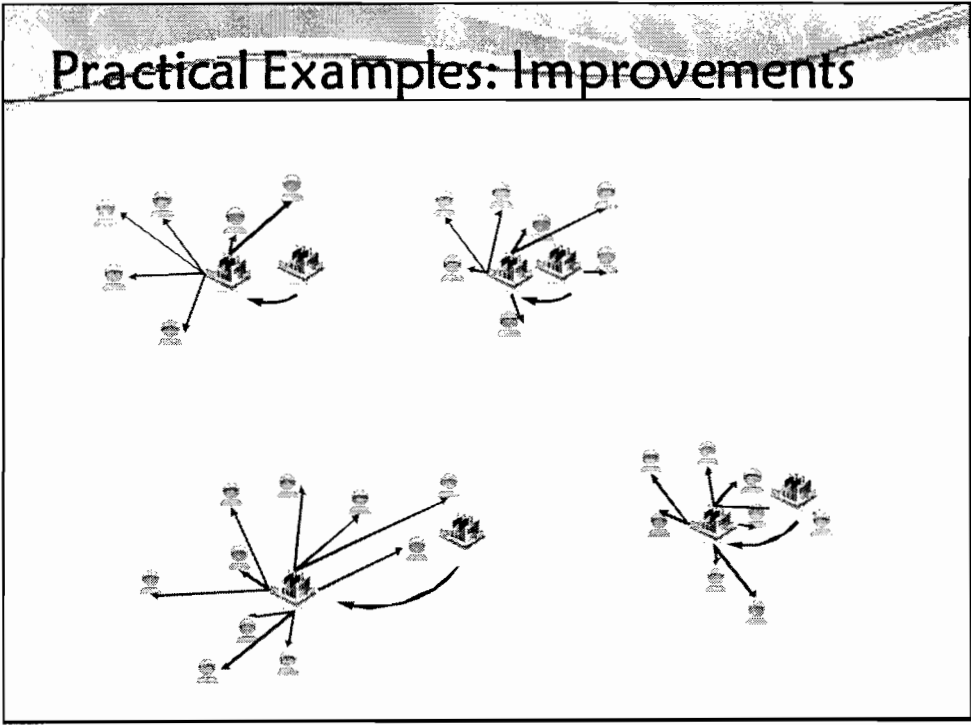
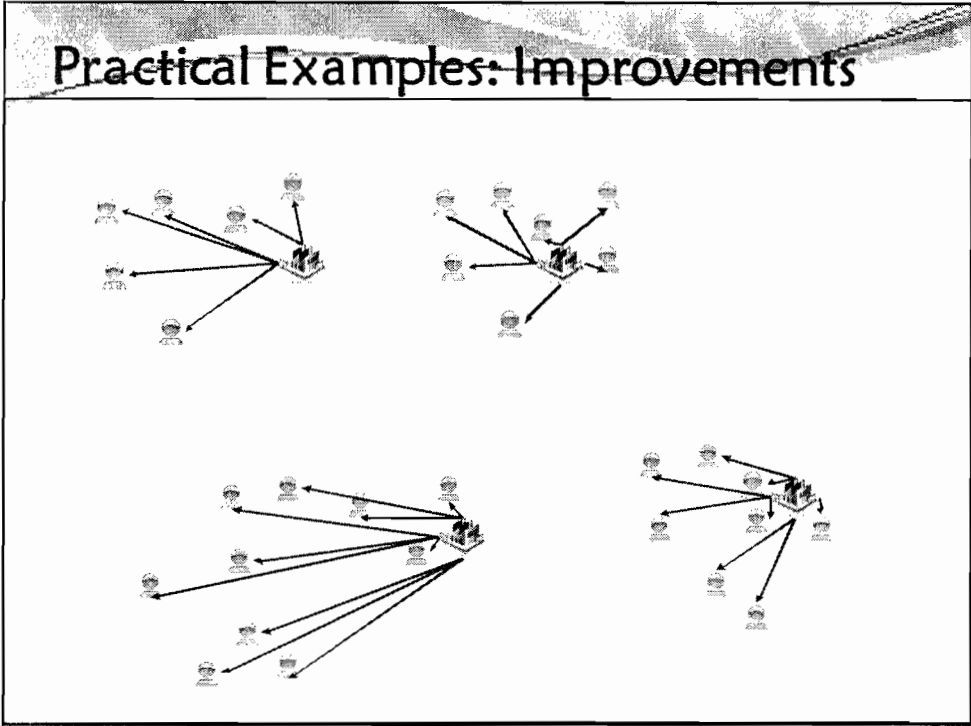


## Practical Examples: A guided

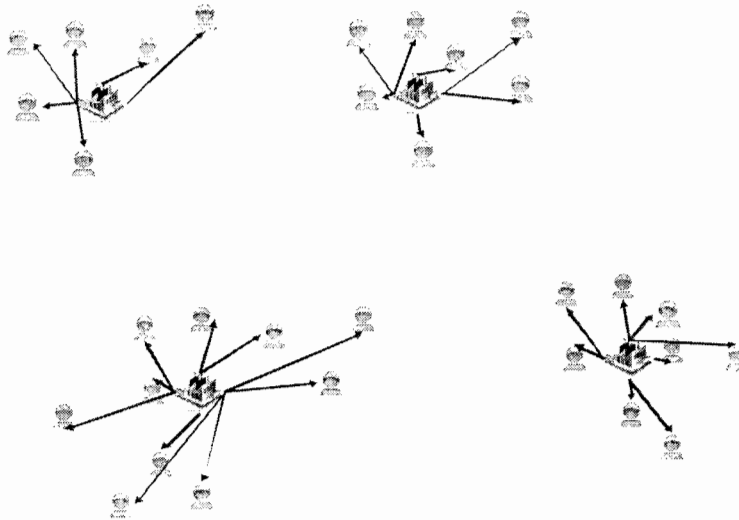


## Practical Examples: Initial Locations

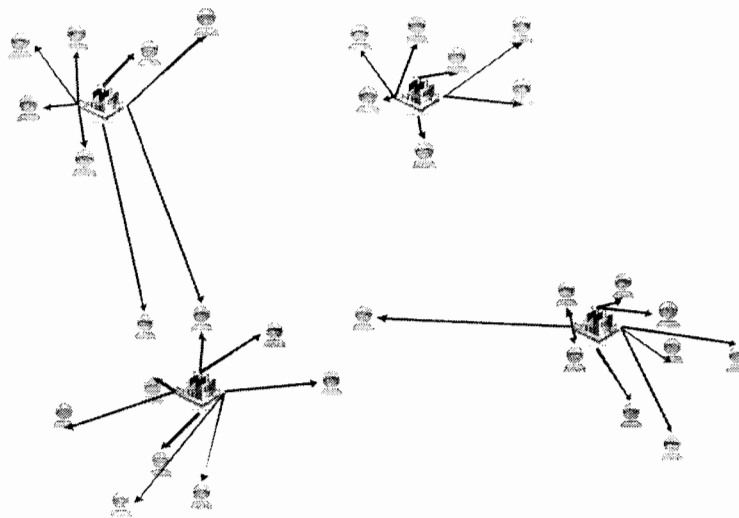




## Practical Examples: Improvements

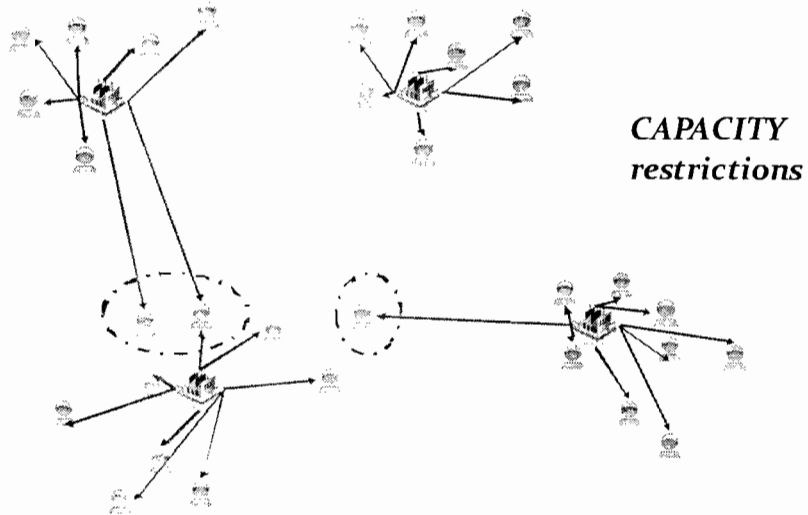


## Practical Examples: "Hot" Issues

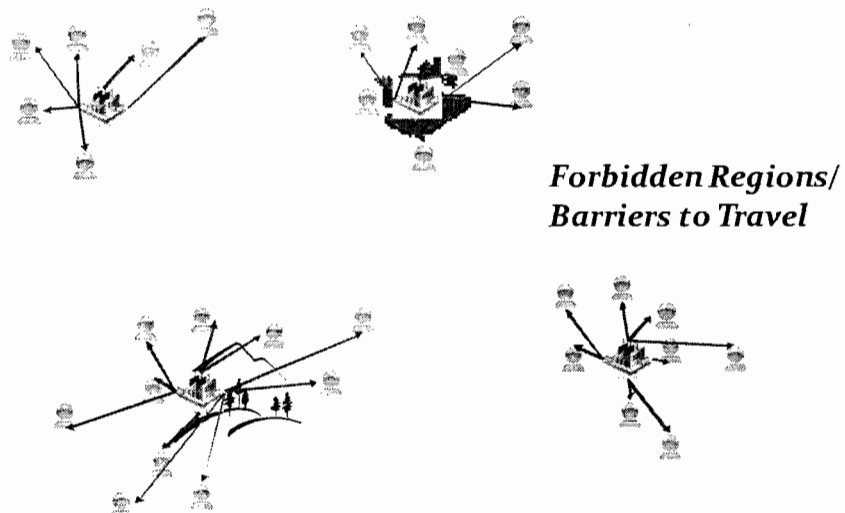




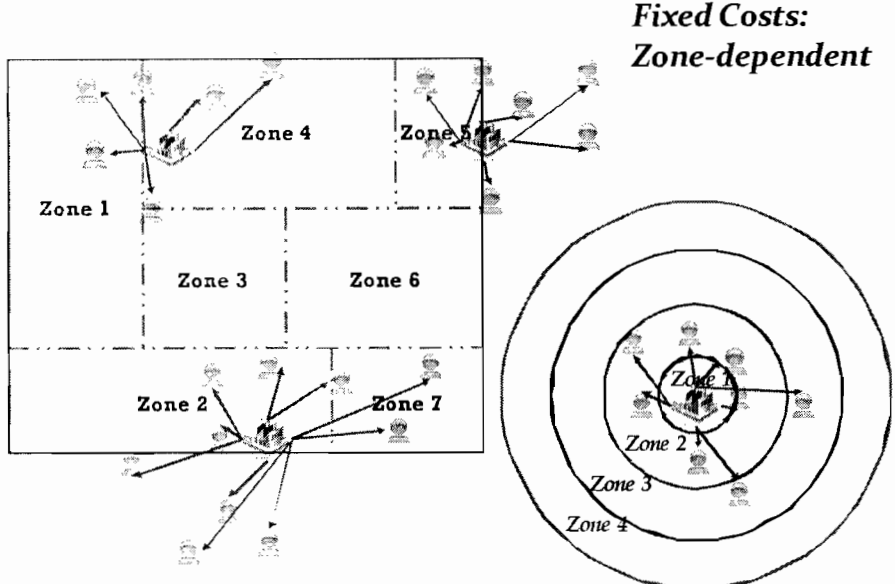
## Practical Examples: "Hot" Issues



## Practical Examples: "Hot" Issues



# Practical Examples: "Hot" Issues



# Future Investigations (1)

			Solution Method		
			Exact Methods	Heuristics	Meta-heuristics
Future Location Problems	Continuous	No Fixed Cost	Kuenne & Soland (1972), Ostresh (1973, 1975), Love & Morris (1975), Drezner (1984), Rossing (1992), Brimberg & Love (1998)	Cooper (1964), Sullivan & Peters (1980), Iyengar & Jud (1982), Miryngal & Niwattayawong (1982), Chen (1983), Bogartz, Calamai, & Conn (1994), Hansen et al. (1998), Lozano et al. (1998), Gamal & Salhi (2001), Tallard (2003), Hsieh & Ten (2004), Aras et al. (2006)	Li, Kao & Wang (1994), Brimberg & Mladenović (1996a, 1996b), Houck, Jones, & Kay (1996), Ohlemüller (1997), Brimberg et al. (2000), Salhi & Gamal (2003)
		Fixed Cost	Brimberg & Salhi (2005)	Brimberg, Mladenović, & Salhi (2004), Brimberg & Salhi (2005)	
		Forbidden Regions & Barriers to Travel	Larson and Sadri (1983), Batta, Ghose, & Parkekar (1989), Aneja & Parlar (1994), Klamroth (2004), Pfeiffer & Klamroth (2005)	Kaz & Cooper (1981), Hansen, Peters, & Thisse (1982), Hamacher & Nickel (1995), Butt & Cavalier (1996), Hamacher & Klamroth (2000), Klamroth (2001a, b), McGarvey & Cavalier (2003), Klamroth (2004)	Bischoff & Klamroth (2007), Canbolat & Wesolowsky (2010)
	Capacitated	Cooper (1972), Sherali et al. (1994, 2002)	Cooper (1972), Zainuddin & Salhi (2006), Aras, Orbay & Altinel (2006), Aras, Altinel & Orbay (2007), Luis et al. (2009)	Gong et al. (1997), Luis et al. (2011)	
Discrete	Capacitated	Sa (1969), Davis & Ray (1969), Akinc & Khumawala (1977), Beasley (1983), Christofides & Beasley (1983), Van Roy (1986), Holmberg, Rönnqvist, & Yuan (1999), Wu, Zhang, & Zhang (2006)	Khumawala (1974), Jacobsen (1983), Domschke & Drexl (1985), Sridharan (1991, 1995), Agar & Salhi (1998), Rönnqvist, Traganterngsak, & Holk (1999), Ahuja, Orlin, Paoonitmo, Scaparra, & Savelli (2004), Wu, Zhang, & Zhang (2006), Klose & Görz (2006)	Delmaire, Fernández, & Ortega (1999), Dias et al. (2006), Liao & Guo (2008)	
On a Line	Capacitated	Love (1976), Mirchandani, Kohli, & Tamir (1996), Brimberg & Mehrez (2001), Brimberg et al. (2001)	Eben-Chaïme, Mehrez, & Markovic (2002)		

## Future Investigations (2)

		Solution Method		
		Heuristic	Metaheuristic	Hyperheuristic
Facility Location Problems	Probabilistic Demands	Forbidden Regions &/ Barriers to Travel		
		Fixed Costs: <ul style="list-style-type: none"> <li>• Zone Dependent</li> <li>• Throughput Related</li> </ul>	RESEARCH	
	Discrete	Forbidden Regions &/ Barriers to Travel		
		Fixed Costs: <ul style="list-style-type: none"> <li>• Zone Dependent</li> <li>• Throughput Related</li> </ul>		
Capacitated	Probabilistic Demands	Forbidden Regions &/ Barriers to Travel		
		Fixed Costs: <ul style="list-style-type: none"> <li>• Zone Dependent</li> <li>• Throughput Related</li> </ul>		

## Future Investigations: A blend of

- *Location Routing Problems (see Nagy and Salhi, 2007)*
  - *A mixture of Location and Routing problems*
  - *the strategic and tactical planning of distribution management problems*
  
- *Inventory Location/ Routing Problems*  
(see Moin, N. H., Salhi, S. and Aziz, N.A.B, 2010)

— THANK YOU  
Very Much for Your Attention —

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